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DAVIDSON LABORATORY

Report 1169



RESPONSE OF SLOWLY MOVING SHIP TO PROPELLER AND RUDDER ACTIONS

> by C. Lincoln Crane, Jr.

> > October 1966

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OCTOBER 1966

RESPONSE OF SLOWLY MOVING SHIP TO PROPELLER AND RUDDER ACTIONS

by

C. Lincoln Crane, Jr.

Prepared for the
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A. Strumpt, Chief

Stability and Control Division

ABSTRACT

An attempt is made to extend ship-maneuvering analysis for application at low ship speeds. Captive-model experiments are made to investigate effects of non-equilibrium propeller speeds on rudder force and effective thrust. Other experiments are made to explore first-order effects of very large drift angles and pure yaw rotation on hull hydrodynamic reactions. The experimental results, together with previous rotating-arm data, are applied in motion equations, accounting for both extreme propeller actions and the occurrence of large drift angles and turning rates. Also included are propulsion and rudder time lags, and the influence of uniform water current on ship trajectory. The equations are programmed for computation, and ship response to a simple docking maneuver is predicted. The computation is repeated several times to examine sensitivity of ship motions and trajectory to variations of operating parameters, namely, maximum reverse propeller speed, engine response time, and water current direction.

KEYWORDS

Ship Control:

Maneuvering Steering

Low-Speed Control

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NOMENCLATURE

The basic nomenclature follows that of SNAME Technical and Research Bulletin No. 1-5. Principal exceptions are the choice of typical dimensions used in forming dimensionless quantities, and the use of additional notation.

Three different right-handed, rectangular coordinate frames are used:

- (x, y, z) are body axes with origin at the center of gravity, x directed toward the bow along the longitudinal centerline hull axis, y directed toward starboard, and z from deck to keel. The x, y plane is horizontal with the ship in static equilibrium.
- 2. (x_0, y_0, z_0) are fixed relative to the earth, with the x_0 and y_0 axes in a horizontal plane and z_0 directed downward. When yaw angle ϕ is zero, the ϕ and ϕ axes are parallel to the ϕ and ϕ axes, respectively.
- 3. (x_I, y_I, z_I) are fixed relative to the body of water, which moves with a constant velocity relative to (x_0, y_0, z_0) . This velocity is called the water current and is denoted \overrightarrow{U}_{C_0} . The x_I, y_I , and z_I axes are always parallel to the x_0, y_0 , and z_0 axes, respectively.

Unless otherwise noted, all dimensionless hydrodynamic (hull) derivatives are evaluated at zero angular velocity and acceleration, zero angles of sideslip and rudder, and propeller speed set for model self-propulsion point. Definitions of symbols used are listed below:

A, A, ..., B, ..., C, etc. Hydrodynamic force and moment coefficients used in motion equations, formed from products of dimensionless coefficients and dimensional quantities ρ , L, H; for example, $B_1 = \rho/2$ LHY.

a, a, .., b, b, .., c, etc. Dimensionless coefficients used in representations of propeller and rudder forces

CG Center of gravity

A propeller thrust coefficient, useful for stalled propeller

	[10] 는 10~gain - 10 Let 10 [20]는 [21 17.77] 2 E. 10 Let 12 Let 12 [20] 2는 10 [20] 2 [21] 2 [21] 2 [22] 2 [
d	Propeller diameter		
91 , 92 , 93	Bounding values of $1/J_s$, distinguishing different regions of propeller operation; used for selecting relevant representation during computation		
F	Vector sum of external forces acting on ship		
Н	Ship draft		
I	Ship inertia tensor		
Iz	Moment of inertia of ship about z axis		
J _s	Propeller advance ratio in behind-ship condition		
k _X ,k _Y ,k _N	Functions used when obtaining propeller and rudder force and moment representations; dimensionless		
L	Ship length, between perpendiculars		
m	Mass of ship		
N	Hydrodynamic moment component relative to z axis; yaw moment		
Ŋ	Vector sum of external moments acting on ship		
n	Propelier speed of rotation		
р	Propeller pitch		
r	Angular velocity component of ship axes in z direction		
rt	Dimensionless angular velocity; r' = rL/U		
rį	Limiting value of r: for cruising-type maneuver		
+	Angular acceleration component of ship axes in z direction		
T	Time constant for propeller-speed response		
t	Time		
So	Apparent slip ratio of propeller		
\$	Distance along trajectory		
U	Speed of CG relative to fluid		
Uco	Speed of water current relative to earth		
u,v	Velocity components of CG relative to fluid, measured in directions of x and y axes, respectively		
u, vI	Velocity components of CG relative to fluid, measured in directions of x_0 and y_0 axes, respectively; (x_I,y_I) and (x_0,y_0) coordinate frames are always parallel		
uo,vo	Velocity components of CG relative to earth, measured in directions of x and y axes, respectively		
uco,vco	Velocity components of water-current relative to earth, measured in directions of x_0 , y_0 axes, respectively		
ů,ů	Acceleration components of CG in directions of x and y axes, respectively		

	행배하셨어? 하나 내용 경영 살보다면 하는 아니까요 경우 내용이라면 하는 사람들이 하는 사람들이 되었다면 하는 사람들이 되었다면 하는데		
X,Y	Hydrodynamic force components relative to x and y axes, respectively; longitudinal and lateral forces		
Y., N.	Typical dimensionless first derivatives of a hydrodynamic force and moment with respect to a velocity component		
Y! , N!	Typical dimensionless first derivatives of a hydrodynamic force and moment with respect to an angular velocity component		
YĮ,NĮ	Typical dimensionless first derivatives of a hydrodynamic force and moment with respect to a linear acceleration component		
AĬ'NĬ	Typical dimensionless first derivatives of a hydrodynamic force and moment with respect to an angular acceleration component		
Yrv,Nrv	Typical dimensionless third derivatives of a hydrodynamic force and moment with respect to an angular velocity component and a lateral velocity component		
X,Y,N(Hull)	Sums of X, Y, N attributed to hull motions, respectively		
X,Y,N (Prop. + Rudde	Sums of X,Y,N attributed to propeller and rudder actions		
β	Drift-angle; sinβ = -v/U		
β_{L}	Limiting drift angle for cruising-type maneuvers		
8	Rudder deflection		
ρ	Mass density of water		
*	Yaw angle, measured about z axis, relative to x axis		
∳c	Direction of water-current flow, measured about z axis relative to x axis		
w	Angular velocity of ship relative to (x _o ,y _o ,z _o) axes		

Subscripts

Referred to axes fixed with respect to earth; also initial time when used with t

Previous steady value

Desired or commanded value

INTRODUCTION

Upon entering pilot waters from seaward, the difficulties in controlling a ship increase enormously because of the proximity of many solid boundaries such as harbour installations and other ships. The extremely low control force to momentum force ratios of large merchant ships is the main factor which makes close quarter maneuvering difficult. To minimize both the danger and damage of collision, it is necessary to drastically reduce ship speed in this type of operations.

However, the reduction of ship speed introduces other problems which complicate ship control. Among these are the effects of wind and current, and the strong dependence of rudder forces on propeller speed (for single screw ships). All these factors combine to cause frequent saturation of propeller and rudder. This accounts for the common use of tugs, bow thrusters, or anchors during close quarter maneuvers of ships.

The work done under the present task order was divided into two phases. In the first phase, the effects of wind on low-speed ship control and stability were treated and reported separately by Eda. 2! The second phase, reported herein, deals with the effects of steady water currents and changing propeller speed. In neither case were the effects of the proximity of solid boundaries on the hydrodynamic forces treated.

The simplified motion equations used in most studies of ship control provide satisfactory predictions of maneuvers under cruising (constant throttle) conditions, but are not sufficiently general to treat many real control problems, such as those which occur at low-ship speeds.

Controllability surveys by Norrbin, ¹ Eda and Crane, ² Williams and Noble, ³ Goodman, ⁴ and Abkowitz ⁵ discuss the usual forms of equations and their solutions. None include propeller-speed changes or water-current effects. Saunders, ⁶ and more recently Hawkins, ⁷ have discussed special low-speed maneuvers without using equations of motion. Crane, Uram and

Chey have formulated motion equations for mooring and docking maneuvers of a destroyer and a submarine. But most efforts on non-equilibrium propeller effects have concentrated on ship-stopping. These works are summarized in Reference 9. Papers by English, 10 Hawkins, 7 Stuntz and Taylor, 11 and others treat bow-thrusters and other maneuvering-propulsion devices (MPD), but these do not include MPD forces in maneuvering analysis.

The present work is an attempt to extend the generality of ship-maneuvering analysis to include engine-maneuver and steady water-current effects, and to introduce the possibilities of very large drift angles and dimensionless turning rates.

Equations of motion are formulated for translation and rotation of a surface ship maneuvering in a reference frame which is fixed with respect to a moving water mass (the water current). The independent ship variables comprise propeller speed and rudder angle. The equations are solved with respect to the coordinate frame moving with the water, and the solution is transformed to a fixed coordinate frame. Resultant ship velocity is integrated to obtain the position and orientation of the ship at any time. Water current is a parameter, and is made zero when discussing other effects.

Coefficients of the equations are obtained from experiment, calculation, and existing data. The combined effects on the hydrodynamic forces and moments of ship speed, propeller speed, and rudder angle (at maneuvering speeds) are investigated by captive-model tests in a straight towing tank. Indications of hydrodynamic reactions to very large drift angles and to pure yaw rotation are obtained experimentally. Numerical integrations are performed by digital computer.

A few examples of computed maneuvers are given to illustrate uses which can be made of more general analyses of ship maneuvering. Using the computation procedure developed, the sensitivity of ship response to particular ship parameters is studied for a simple ship-docking maneuver.

It is noted that some of the procedures used in formulating the

equations of motion are merely expedient measures taken to permit qualitative results to be obtained. More fundamental treatment of tiese closequarter, low-speed control problems is left for future studies.

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EQUATIONS OF MOTION - GENERAL

General Form of Motion Equations

Differential equations describing the motion of a ship are written with respect to a reference frame rotating with the ship's axes, the origin of which is chosen coincident with ship's center of mass (see Figure !).

$$\vec{F} = m(\frac{d\vec{V}}{dt} + \vec{\omega} \times \vec{V})$$

$$\vec{N} = I \frac{d\vec{\omega}}{dt} + \vec{\omega} \times \vec{I} \vec{\omega}$$
(1)

where

F sum of all external forces

N sum of all external moments

V velocity of ship center-of-mass

พื่ angular velocity of ship (ship's axes)

I moment of inertia tensor

All vectors can be expressed in rotating (ship axes) coordinates. For a surface ship in calm water, hese vector equations are reduced to three Cartesian equations by applying the following simplifying assumptions:

- 1. Ship is constrained to move in its lateral plane (i.e., the x, y-plane), which is horizontal.
- 2. Center-of-mass is in the principal plane of symmetry of the hull.
- 3. Mass and center of mass are constant.
- 4. Products of inertia are zero.

Then,

$$m(\mathring{\mathbf{u}} - r\mathbf{v}) = X$$

$$m(\mathring{\mathbf{v}} + r\mathbf{u}) = Y$$

$$I_z\mathring{\mathbf{r}} = N$$
(2)

where X and Y represent summations of unbalanced external forces acting in the x and y directions, and N the summation of unbalanced moments about the z-axis.

External forces arise from hydrodynamic reactions to hull motion, propeller and rudder actions, aerodynamic reactions on hull structure, and all other forces which may be applied by waves, bow-thruster, anchor chain, tugboat, mooring lines, etc. In this analysis, only hull hydrodynamic and propeller-rudder forces are included. In succeeding sections, their contributions to X, Y, and N are considered.

Reference Frames

It is clearly desirable to describe low-speed ship maneuvers relative to an inertial reference frame fixed in the earth. However, the motion equations and solution are greatly simplified if referred to a coordinate frame fixed in the ship, with subsequent transformation of solutions to the desired reference frame (Figure 1).

With a uniform water current, an additional (intermediate) reference frame is useful. The additional frame maintains the same orientation as the fixed frame, but moves with the steady velocity of the uniform water current. In computation, the first transformation of the solution is from ship axes to intermediate axes. The second transformation simply adds the water-current velocity components, to obtain motions relative to the final desired reference frame.

It is emphasized that the uniform water current need not enter the differential equations of motion, because a steady velocity will introduce no acceleration in the motion equations. The current is entirely accounted for in the final integration of velocities. Steps involved in the velocity transformations are shown below

(1) Ship velocity components (expressed in ship axes) are transformed to intermediate axes by a rotation of coordinates.

$$u_{I} = u \cos \psi - v \sin \psi$$

$$v_{\tau} = u \sin \psi + v \cos \psi$$
(3)

^{*}Orientation of ship axes with respect to ship geometry varies according to ship loading conditions because, for convenience, x and y ship-axes are taken horizontal (hence, z-axis vertical).

and
$$\psi = \int_0^t rd\tau + \psi(0)$$

where

 υ and υ are coordinates of velocity along ship axes, and υ_{I} and υ_{I} are components of ship velocity along intermediate axes

(2) Components of water-current velocity are then added to obtain ship motion relative to fixed inertial axes.

$$u_o = u_I + u_{c_o}$$
 $v_o = v_I + v_{c_o}$

or

$$u_{o} = u \cos \psi - v \sin \psi + U_{c} \cos \psi_{c}$$

$$v_{o} = u \sin \psi + v \cos \psi + U_{c} \sin \psi_{c}$$
(4)

keeping in mind that the intermediate axes (I) and fixed inertial axes (o) are parallel.

Time integration of the velocities u_0 and v_0 yields instantaneous ship position (x_0,y_0) with respect to any chosen origin.

HULL CONTRIBUTIONS TO EXTERNAL FORCE AND MOMENT

Hydrodynamic forces exerted on a ship's hull are attributed to viscous and inertial fluid effects which are expressed as functions of hull motions and accelerations. Since a wide range of maneuvering motions may occur at low ship speeds, hydrodynamic representations are separated according to application to cruising-type or docking-type maneuvers. The former case is considered first.

A convenient form for expressing hull hydrodynamic forces is available in the Taylor series expansion. ¹² In the present analysis, the general expansion is specialized to the surge, sway, and yaw metions of a ship.

The following simplifications, extra to those noted in the previous section, are made:

- 1. The hydrodynamic derivative coefficients X', X', Y', and N! are assumed to be negligible. For convenience a term proportional to uU is used to account for X' and drift-angle effects.
- Hydrodynamic terms of order four and higher are assumed to be negligible.
- Forces due to hull motions and accelerations are represented to be independent of propeller and rudder actions.
- 4. Ship floats in deep (D/H > 3.5), calm, unrestricted water.

Simplification (3) is necessary due to the absence of captive-model experimental data for a ship on curved path with reversed propeller rotation, or in any propeller condition far removed from model or ship self-propulsion point. An indication of the effects of non-equilibrium propeller speed on hull hydrodynamic data was obtained by inspection of rotating-arm tests results of a model of T.S. EMPIRE STATE IV. 13 The measured effects cannot be explained simply on the basis of propeller-side-force changes at different propeller loadings. Although the differences are large enough to warrant further investigation, they are assumed to be of second-order importance for present purposes.

With the preceding simplifications, the nonlinear hull force-and-moment expressions, retaining third-order terms in the velocities, may be written as

$$X_{hu11} = A_0 u + A_1 u + A_2 v$$

$$Y_{hu11} = B_0 v + B_1 u v + B_2 u v + B_3 v^2 / u + B_4 v^2 v / u + B_5 v^3 / u + B_6 v^3 / u$$

$$N_{hu11} = C_0 v + C_1 u v + C_2 u v + C_3 v^2 / u + C_4 v^2 v / u + C_5 v^3 / u + C_6 v^3 / u$$
(5)

where it has been assumed that |v/u| < 0.26 and r' < 1.0, and

$$A_{0} = \frac{\rho}{2} L^{3} H X_{0}^{I} \qquad B_{0} = \frac{\rho}{2} L^{2} H Y_{0}^{I} \qquad C_{0} = \frac{\rho}{2} L^{4} H N_{0}^{I}$$

$$A_{1} = \frac{\rho}{2} L H X_{0}^{I} \qquad B_{1} = \frac{\rho}{2} L H Y_{0}^{I} \qquad C_{1} = \frac{\rho}{2} L^{2} H N_{0}^{I}$$

$$A_{2} = \frac{\rho}{2} L^{2} H X_{0}^{I} \qquad B_{2} = \frac{\rho}{2} L^{2} H Y_{0}^{I} \qquad C_{2} = \frac{\rho}{2} L^{3} H N_{0}^{I}$$

$$B_{3} = \frac{\rho}{4} L^{2} H (Y_{0} Y_{0}^{I} + Y_{0}^{I}) \qquad C_{3} = \frac{\rho}{4} L^{3} H (N_{0} Y_{0}^{I} + N_{0}^{I})$$

$$B_{4} = \frac{\rho}{4} L^{3} H Y_{0}^{I} \qquad C_{4} = \frac{\rho}{4} L^{4} H N_{0}^{I}$$

$$B_{5} = \frac{\rho}{12} L^{4} H Y_{0}^{I} \qquad C_{5} = \frac{\rho}{12} L^{5} H N_{0}^{I}$$

$$B_{6} = \frac{\rho}{12} L H (Y_{0} Y_{0}^{I} + 3 Y_{0}^{I}) \qquad C_{6} = \frac{\rho}{12} L^{5} H (N_{0} Y_{0}^{I} + 3 N_{0}^{I})$$

All dimensionless coefficients except X_{U}^{I} , X_{V}^{I} , Y_{V}^{I} , and N_{I}^{I} are evaluated experimentally, as described in Reference 13.

The derivatives X_{U}^{1} , Y_{V}^{1} , and N_{r}^{1} relate hydrodynamic forces to hody accelerations, and X_{Vr}^{1} is taken equal in magnitude to Y_{V}^{1} . The Y_{V}^{1} and N_{r}^{1} coefficients are computed following the method of Lewis 14 and Prohaska. For example,

$$-Y_{\cdot}/m = \frac{\frac{1}{2} m_{c} \int_{x_{b}}^{x_{s}} k_{x}(x)H^{2} dx}{\int_{x_{b}}^{x_{s}} s(x)dx}$$

In this strip-wise integration, $k_{_{\mathbf{X}}}$ is the two-dimensional lateral added-

mass coefficient. This is determined for ship-like sections, by using Prohaska's results. The $k_{\rm C}$ is a three-dimensional correction factor determined by comparing the exact added-mass computation of the prolate spheroid given by Lamb with that obtained by the stripwise computation for the same spheroid. Factor S(x) is the local sectional area. The rotary acceleration derivative $N_{\rm F}^{\rm I}$ is obtained in a similar manner, but includes an x^3 factor in the integrand of the numerator. The longitudinal acceleration derivative $X_{\rm L}^{\rm I}$ is taken equal to that of an equivalent prolate spheroid.

Conditions at Very Low Speeds

Experience shows that at moderate ship speeds, drift angle, β , does not normally exceed approximately ± 10 degrees, and dimensionless turning rate, r', is normally limited to about 0.7 (corresponding to turning-diameter/ship-length \approx 3). However, a ship maneuvering at very low speeds may develop much larger drift angles and space turning rates.

Consider the definition of $\,\beta$, as forward speed $\,u\,$ becomes small with respect to lateral speed, v :

$$\lim_{u\to 0} \beta = \lim_{u\to 0} \left[-\tan^{-1} \left(\frac{v}{u} \right) \right] = \pm \pi/2$$

In similar fashion, space turning rate grows large as ship speed vanishes;

$$\lim_{U \to 0} r! = \lim_{U \to 0} \frac{rL}{U} \to \infty$$

Such situations arise with the action of external forces which are not wholly dependent on ship motions.

Two broad categories of maneuvers are defined:

- Cruising-type maneuvers: Both of the below criteria are satisfied.
- Docking-type maneuvers: One of the below criteria is unsatisfied, or both are unsatisfied.

$$|\beta| < \beta_L$$
 $|r'| < r'_L$

These definitions are useful in defining maneuvers for which conventional hydrodynamic expansions are valid. These are called cruising-type maneuvers, and it is for these that most experimental data are obtained. Ranges of variables may be extended to cover docking-type maneuvers, of course (given sufficient date), but it is possible that an expansion other than Taylor's series may be more convenient for treating docking-type maneuvers (double Fourier series, for example). If a Taylor series is used, an expansion point at $(u=v=r=\hat{u}=\hat{v}=\hat{r}=0)$ might prove more convenient than at (u=u), $v=r=\hat{u}=\hat{v}=\hat{r}=0)$.

In this report an example of a simple docking maneuver is computed. The maneuver is terminated as forward motion stops after sustained reversed propeller action. The computation will show a tendency for the ship to develop large values of β and r' at the end of the maneuver. To allow for this, terms exhibiting first-order qualities of the true (steady-state) hydrodynamic reactions are used in this region. Coefficients of the simplified terms are relatively easy to evaluate, since they represent uncoupled drift-angle and yaw-rate effects. The acceleration dependent terms appear as before. Simplifications 3 and 4 still apply.

$$X_{hu11} = A_0 u + A_1 u U + A_2 r v$$

$$Y_{hu11} = B_0 v + B_7 v U + B_8 v |v| + B_9 u r$$

$$N_{hu11} = C_0 r + C_7 v u + C_8 \frac{v u}{U^2} |v u| + C_9 r |r|$$
where it is assumed that $u > 0$.

The relative importance of steady-state hydrodynamic forces obviously declines (relative to inertia effects) as ship speed decreases. However, it cannot simply be stated that steady-state terms are negligible below any particular speed (except under very special conditions). For example, consider ship response to a pure applied yaw moment. After initial yaw acceleration, the resisting hydrodynamic moment is almost entirely a steady-state damping effect. If steady-state terms were arbitrarily excluded, acceleration without limit would be computed.

PROPELLER AND RUDDER CONTRIBUTIONS TO EXTERNAL FORCE AND MOMENT

An important departure from usual maneuvering analyses, at low ship speeds, is the loss of proportionality between control forces and the hull forces which are associated with motion through the water. The control forces of propeller and rudder can be disproportionately large or small, according to the action of the propeller. External forces and moments attributed to propeller and rudder actions depend on several factors including

- 1. Propeller, hull, and rudder configurations
- 2. Propeller speed of rotation and angular acceleration
- 3. Ship linear and angular velocity
- 4. Rudder angular deflection and deflection rate
- 5. State of cavitation or ventilation of propeller and rudder
- 6. Ship hydrodynamic environment, i.e., water density, depth, and lateral boundaries, and waves

The following assumptions, together with those in previous sections, simplify representations of propeller and rudder forces:

- 1. Ship speed is low; hence lateral ship velocity is small.
- 2. Yaw rotation is slow.
- 3. Based on (1) and (2), the lateral component of inflow to propeller and rudder is small.
- 4. Rudder deflection rate is slow, conforming to normal ship practice (2-1/20/sec). Also, frequency of rudder oscillation is low; hence errors due to quasi-steady representation are small.
- 5. Accelerations of propeller rotation, rudder deflection, and hull motion which might affect propeller and rudder forces have negligibly small effects on integrated hull motions.
- 6. Propeller and rudder are not cavitating.

With the above assumptions, propeller and rudder forces are represented as functions of propeller speed, n ,ship's longitudinal speed, u , and rudder angular deflection, δ .

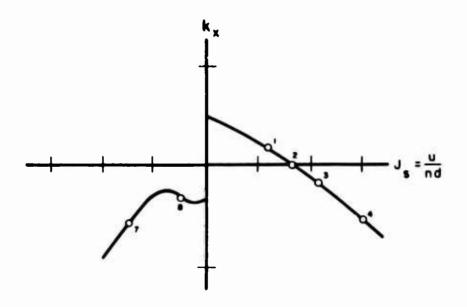
X Force Due To Propeller and Rudder

The dimensionless thrust coefficient, $k_t = \frac{thrust}{\rho d^4 n^2}$, is commonly used to represent propeller test results for various conditions of ship speed and propeller rotation. This notation is useful as an aid in understanding and representing propeller force effects. In this study, self-propelled captive-model tests have been used to measure a quantity which will be denoted X(prop.4 rudder). This quantity is defined as total measured axial force, $X(u,n,\delta)$, minus the resistance of the model hull without propeller, X(u,-,-). From this, a dimensionless "effective thrust" coefficient is defined.

$$k_{x} = \frac{X(u,n,\delta) - X(u,-,-)}{\rho d^{4} n^{2}}$$
 (7)

As with open-water propeller thrust characteristics, it is convenient to graph k_x as a function of propeller advance ratio (here using ship's speed of advance), i.e., $J_s = \frac{u}{nd}$. For clarity, rudder effects are omitted from the next discussion.

Sketch I shows the relation of k_{X} to J_{S} in regions of propeller operation which are important for ship-stopping.

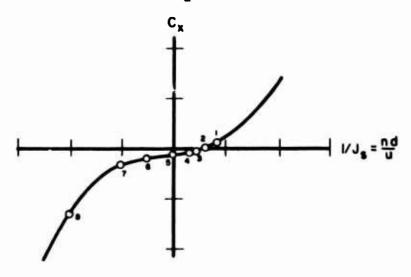


SKETCH I

The path of k_{χ} during rapid propeller-reversal is traced:

- Approach to equilibrium condition (thrust = resistance)
- Propeller speed reduced; blade sections approach zero angle of attack (thrust zero)
- 3. Propeller speed further reduced; blade sections at negative angles of attack (thrust negative)
- 4. Propeller speed further reduced; flow about blades completely separates (propeller dragging)
- 5. Propeller stopped and dragging, ... 6. Propeller turning slowly astern but dragging
- 7. Astern propeller speed increased (blades recover from stall and begin thrusting astern)
- 8. Propeller speed approaches a constant value; ship speed gradually reduces; astern thrust determined by propeller characteristics

The representation of Sketch I is not useful in the interval between 4 and 7. Mathematically, as an approaches zero, J_s tends to infinity. Furthermore, beyond the blade stall-point at large negative angles of attack, k_x cannot be represented simply in terms of J_s . For cargo ships and tankers the negative blade-angle stall will occur at a J_s value between 2 and 4. Another dimensionless coefficient is then convenient to express "effective propeller thrust." This is the coefficient $c_x = \frac{\chi}{\rho \, d^2 \, u^2}$, used by Bindel 16 and others. The singularity in $J_s = \frac{u}{nd}$ is avoided by using the reciprocal, $\frac{nd}{u}$.



SKETCH II

The characteristic behavior of c_{χ} in a ship-stopping maneuver is shown in Sketch II (numbers correspond to those of Sketch I). Because propeller speed will change much more quickly than ship speed, the behavior of X(prop.) is similar to that of c_{χ} in Sketch II.

Because of slow propeller speeds in the region from 4 to 6, experimental evaluation of $c_{\rm X}$ is subject to serious scale effect (especially for propeller operating behind the ship); but if $c_{\rm X}$ passes from 4 to 6 in a few seconds, the accuracy of the representation in this region is not crucial. An estimated propeller drag coefficient is therefore used (See Appendix A).

When unstalled propeller operation resumes (at some reversed propeller speed), the k_x vs. J_s relation is again effective and simple to use. The required segments of the k_x , J_s curve are easily described by simple polynomials in J_s . For example, in the region from 1 to 4 (of Sketch I), an adequate curve-fit is obtained using $k_x = a_0 + a_1 J_s + a_2 J_s^2$. And since

$$X(prop) = k_x pd^4 m^2$$

substitution of the polynomial in J_s for k_x , and $\frac{u}{nd}$ for J_s , yields

$$X(prop) = (pd^4 a_0)n^3 + (pd^3 a_1)un + (pd^2 a_2)u^3$$
 (8)

where a_0 , a_1 , a_2 are determined for a particular propeller and hull.

In similar fashion, the $k_{_{\boldsymbol{X}}}$ curve segment passing from point 7 through point 8 may be curve fitted to $J_{_{\boldsymbol{S}}}$. For digital computation of maneuvers, the correct expression for $k_{_{\boldsymbol{X}}}$ can be automatically selected according to the instantaneous value of $J_{_{\boldsymbol{E}}}$, using rules based on Sketch I.

Rudder effect on X force is treated next. The drag of a rudder mounted aft of an ahead-turning propeller is a function of rudder angle, ship speed, and propeller speed. If k_{χ} is approximately parabolic with rudder angle, δ , a simple extension of the propeller-thrust representation to rudder drag may suffice.

$$X(rudder) = k_{x \cdot \delta} \rho d^4 n^2 \delta^2$$
 (9)

Here we express $k_{x,\delta} = a_3 + a_4 J_s$, leading to

$$X(rudder) = \left[(\rho d^4 \ a_3) n^2 + (\rho d^3 \ a_4) un \right] \delta^2$$
 (10)

When propeller is dragging or reversed, the rudder drag is small and erratic. No attempt is made to represent it.

Y Force Due to Propeller and Rudder

Representations of Y force and N moment due to propeller and rudder closely follow those for X force. The following will pertain to both Y and N .

Because the flow past the rudder (of a single-screw ship) is determined by both ship speed and propeller speed, the concept of $k_X vs. J_S$ is useful for developing a polynomial representation for side force, but now only in the propeller operating region from 1 to 4 of Sketch I. If in this region Y is a linear function of rudder angle, the symmetrical part of Y(prop. + rudder) with respect to δ may be represented by

$$[(pd + b_0)n^2 + (pd^3 b_1)un + (pd^2b_2)u^2]\delta$$

A small unsymmetrical side force is also observed for single-screw ships. This is called the Hovgaard effect and is caused by asymmetry of propeller rotation. Several authors attempt to explain this physically, but it is represented here as a simple function of u and n, based on results of straight course experiments in the next section. Summing the symmetrical and unsymmetrical parts, the total expression is

Y(prop. + rudder)=
$$[(\rho d^4b_0)n^2+(\rho d^3b_1)un+(\rho d^2b_2)u^2]\delta+(\rho d^4b_3)n^2+(\rho d^3b_4)u^3$$
(11)

In the stalled region, for advance ratios to the right of point 4, flow aft of the propeller is much disturbed. Rudder forces are then sharply reduced and difficult to evaluate. In this condition, it is estimated that rudder effectiveness is reduced to less than 1/3 of that in normal ahead operation. This is based on model tests of a related single-screw hull with propeller removed.

As propeller rotation is reversed the propeller race is directed forward. Local flow past the rudder is destroyed and steering control is lost. Side-force bias due to propeller rotation gains importance, and it alone influences the directional behavior of the ship (in the absence of

other external forces).*

N Moment Due to Propeller and Rudder

The representation of yaw moment produced by propeller and rudder, N(prop.+rudder), closely follows that for side force. An additional length dimension appears in the exponent of d. The number of terms in J_s will depend upon the shape of the function k_N , and the precision required.

A summary of terms used in the present study for N(prop. + rudder) appears below:

Operating Region of Propeller	Expression for Rudder-Propeller Yaw Moment	
1 to 4	$N_{\delta,n} = (\delta q_{2}c^{0}u_{5} + \delta q_{4}c^{1}nu + \delta q_{3}c^{3}n_{5})\delta + \delta q_{2}c^{3}u_{5}$	(12)
4 to 6	$N_{\delta,n} = \rho d^3 c_4 u^2 \delta$	(13)
6 to 8	$N_{\delta,n} = \rho d^{5} c_{5} n^{2}$	(14)

Although insufficient data are available to analyze ship dynamic stability in this condition, the reversed propeller may destabilize the ship by its effect on the flow about the hull. While this could cause yaw divergence in either direction, at low speeds the unbalanced side force produced by the reversed propeller usually causes yaw angle to de /elop in the positive (clockwise)sense. This tendency is shown in later computations. The yaw effect is used to advantage by ship-handlers and explains their preference for port-side-to-pier landings.

TIME LAGS OF PROPELLER AND RUDDER RESPONSE

Engine Orders

Commands from the bridge to engine-control indicate desired magnitude and sense of propeller rotation.* A typical engine-order (bell) table for a merchant ship is shown:

Engine Order	Propeller Speed (rpm)	
Full Ahead	60	
Half Ahead	40	
Slow Ahead	20	
Dead 31ow Ahead	10	
Stop	0	
Slow Astern	-15	
Half Astern	-30	
Full Astern	-45	

The system used aboard naval ships is slightly different. In the naval system, the engine (propeller) is specified, followed by the desired sense and speed of rotation (in thirds). For this study a merchant ship is assumed.

Engine response to orders requiring large amounts of power is limited by the steam pressure available. Minimum allowed levels are established to protect the boiler against excess steam drain through the astern turbine. These limits guide throttle opening until desired propeller speed is approached.

Bridge control is not treated here, but may be introduced immediately, since there is no restriction to discrete propeller speeds in this analysis.

Propeller Time Lag

Rate of change of propeller speed will depend upon

- 1. Instantaneous propeller speed, n
- 2. Instantaneous longitudinal speed, u
- 3. Previous steady propeller speed, n_i , and nozzle combination
- 4. Propeller-speed ordered, n

A complete analysis of transient propeller speed (including propulsion-machinery characteristics and human-response factors) are beyond the scope of the present study. A simplified function is used, which provides a good approximation for the purposes of this work. It is based on full-scale ship data for the "crash-back" maneuver. Propeller response is described by the first-order differential equation $\frac{dn}{dt} + c_1 n + c_2 = 0$. Applying boundary conditions $n = n_0$ at $t = t_1$ and $n \to n$ as $t \to \infty$, instantaneous propeller speed is given by

$$n = n_i + (n* - n_i)(1 - e^{-\Delta t/T})$$
, $\Delta t = t - t_i$ (15)

where T = time constant for particular ship and maneuver. This may be estimated by fitting Equation (15) to given response data.

Rudder Time Lag

The steering machinery of a large ship will provide approximately constant rudder rotation for rudder changes of more than a few degrees. According to U.S. Coast Guard Marine Engineering Regulations and American Bureau of Shipping Rules, average rudder rotation shall not be less than 2-1/3 degrees per second. In the S.S. GOPHER MARINER trials, the rudder was shifted from 35° left to 35° right in 22 seconds, i.e., at an average rate of 3.2 degrees per second.

For constant rudder angular rate, rudder deflection is represented by $\delta = \delta_i + \dot{\delta}(t-t_i)$, and $\delta \gtrsim \delta^*$ according to sense of rotation, where

 δ_i = initial deflection angle

t; = time at execution

 δ = rudder angular rate

 δ^* = ordered rudder angle

The sign of δ is determined by the sign of $(\delta^* - \delta_i)$. Rudder-angle commands are specified in degrees right or left of amidship (- or + , respectively), but radian measure is used in equations.

SUMMARY OF MOTION EQUATIONS

The equations of motion are summarized below in a form for solutions

X EQUATION

Y EQUATION

$$(m - B_0)^{\circ} = \begin{cases} B_1 uv + (B_2 - m)ur + B_3 rv^2/u + B_4 r^2v/u + B_5 r^3/u + B_6 v^3/u + B_6 v^3/u + B_6 r^3/u + B_6 v^3/u + B_6 r^3/u + B_6 r^3/$$

N EQUATION

$$(I_{2}-C_{0})^{\frac{1}{6}} = \left\{ \begin{array}{ll} C_{1}uv + C_{2}ur + C_{3}rv^{2}/u + C_{4}r^{2}v/u + C_{5}r^{3}/u + C_{6}v^{3}/u & , \beta < \beta_{L}, r^{1} \leq r_{L}^{1} \text{ and } u \geq u_{L} \\ C_{7}vu + C_{8}vu|vu|/U^{2} + C_{9}r|r| & , \beta > \beta_{L}orr^{1} > r_{L}^{1} \text{ or } u < u_{L} \\ \\ + \left\{ \begin{array}{ll} C_{10}n^{2} + (C_{11}n^{2} + C_{12}un + C_{13}u^{2}) \delta & , & 1/J_{s} > g_{1} \\ C_{14}u^{2}\delta & , g_{1} \geq 1/J_{s} > g_{2} & N(Prop + Rudder) \\ \\ C_{15}n^{2} & , g_{2} \geq 1/J_{s} \end{array} \right.$$

Equations (16)

and

$$n = n_{ij} + (n^{k} - n_{ij})(1 - e^{-\Delta t/T})$$
; $\Delta t = t - t_{ij}$ (17)

$$\delta = \delta_1 + \delta(t - t_1) , \quad -\delta_1 \le \delta \le \delta_1$$
 (18)

where

Ship motions, position and orientation relative to earth-fixed axes are provided by

$$u_{o} = u \cos \phi - v \sin \phi + U_{c_{o}} \cos \phi_{c}$$

$$v_{o} = u \sin \phi + v \cos \phi + U_{c_{o}} \sin \phi_{c}$$

$$r_{o} = r$$
(19)

$$x_{o} = \int_{0}^{t} u_{o} dt + x_{o}(o)$$

$$y_{o} = \int_{0}^{t} v_{o} dt + y_{o}(o)$$

$$\phi = \int_{0}^{t} r dt + r(o)$$
(20)

EXPERIMENTAL PROGRAM

Experiments were made to evaluate coefficients of the motion equations. The program was divided into three parts, according to the facilities used. Since the number and ranges of variables are extensive, the test programs were limited to conditions necessary for application of the equations to particular maneuvers.

PROGRAM I: Straight-Course Experiments

A 14-ft captive model was towed at various speeds. Propeller speed was varied among positive and negative values, and rudder deflection was set at intervals between plus and minus 30 degrees. A Series 60 model was used, particulars of which are given in Table 1.

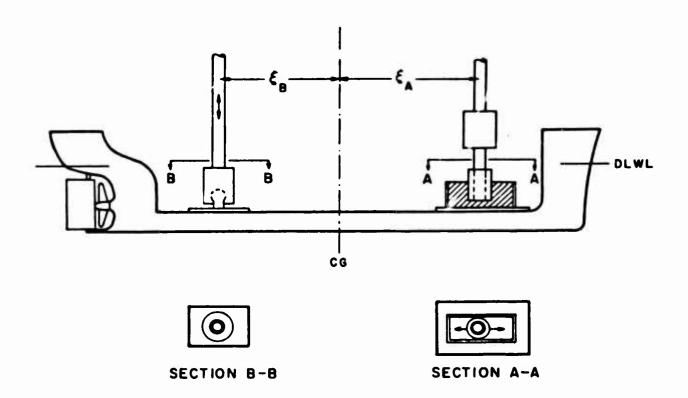
The propeller was driven by a frequency-controlled synchronous motor, integral with a propeller thrust and torque dynamometer. The power source and speed controller were located ashore and connected electrically to the model through overhead cables via the towing carriage.

Rudder deflections were set manually, using a tiller and protractor.

The three force components measured were the longitudinal component X (in line with the model's longitudinal centerline) and the two lateral components Y_A and Y_B (perpendicular to the model's centerline, forward and aft). The net side force is $Y = Y_A + Y_B$. The net yaw moment (acting about a vertical axis through the model CG) is determined by $N = Y_A \times \xi_A + Y_B \times \xi_B$, where ξ is the longitudinal separation between the model center of mass and the force-measuring balances $(\xi_A > 0, \xi_B < 0)$.

The force balances are of the differential transformer type, capable of measuring two orthogonal force components and a moment component about a central axis. Balance locations and constraints are shown in Sketch III on the following page. The model was constrained against surge, sway, and yaw motions, but was permitted freedom to heave, pitch and roll.

SKETCH III



Tests in this program were conducted on straight path (r!=0) with no drift angle (v=0). Model speed, u, was varied between 0 and 5.7 feet per second. Propeller speed was varied between ± 7.65 revolutions per second. No data are reported for propeller speeds less than 4.4 rps, for reasons of scale effect on forces. Rudder angles were limited to ± 30 degrees, because of the effect of scale difference on the point at which rudder stall occurs (near 30 degrees).

Turbulence stimulation (of flow about the hull) was aided by a 0.03-inch-diameter trip wire located 8.4 inches aft of the forward perpendicular. It is unlikely that turbulent flow was achieved at most of the hull speeds of this test. However, hull resistance at low speeds is not significant compared with thrust forces. Furthermore, hull resistance is deducted from the total measured X-force in arriving at thrust coefficient information for use in ship-motion computations; thus, the error introduced is subsequently subtracted.

Hydrodynamic force and moment data are listed for various conditions

of ship speed, propeller speed, and rudder angle (u, n, δ) , in Table II. These data are dimensional for the 14-foot-long model.

The data are reduced to coefficient form in Table III. The dimensionless coefficients are defined in the section on propeller and rudder forces or the section on hull forces. Apparent slip ratio, S_{0} , is given by

$$s_0 = \frac{pn - u}{pn}$$

Coefficient data are plotted in Figures 2, 3 and 4.

PROGRAM II: Large Drift-Angle Experiments

A 5-ft captive model was towed at various drift angles through a total range of 360 degrees. A Series 60 model was used, particulars of which are given in Table I. To avoid wall effects, the tests were conducted in Davidson Laboratory Tank No. 2, with the rotating arm at its longest practical radius. Side force and yaw moment were measured through the entire range of drift angles. Since coupling effects of propeller and rudder should be small relative to hull forces, they were neglected in the test. The propeller and rudder were both fixed.

The model was attached to the rotating arm in a manner similar to that used in conventional rotating-arm experiments of surface-ship models. The principal difference was that the flexure plate mounting on the model was made rotatable in steps of 60 degrees. This extended the drift-angle capability of the balance beyond the usual ± 30 -degree limits, to any desired angle. The normal arrangement, with fixed mounting, constrains the model against yaw, surge, sway, and roll motions, but permits freedom to pitch and heave. The modification changes the nature of the roll and pitch constraints; but negligible tendency to pitch or roll was detected at the low model speeds tested.

Model speed was selected according to the drift angle of the run. For drift angles near 0 or 180 degrees, speeds between 1.5 and 2.5 feet per second were used. At large drift angles, the speed 0.85 feet per second was used, to avoid unrealistically high Froude numbers in conditions that would exist only at very low ship speeds. Speed effect at

90 degree drift angle received special attention. The dimensionless side force coefficient $Y' = \frac{Y}{\frac{\rho}{2} \text{ LHU}^2}$ is plotted against speed for this condition, in Figure 5.

Measurements comprised X and Y components of hydrodynamic force and N component of hydrodynamic moment. Dimensionless coefficients N', X' and Y' are formed, and plotted in Figures 6, 7 and 8, respectively. The rotating-arm facility imposed a small path curvature in all tests of this program. This effect was suppressed by averaging data taken at positive and negative drift angles. Averaged data are represented in the figures. In view of the symmetry of the averaged data, drift-angle arguments in the figures are shown only from 0 to 180 degrees. Ideally, the drift angle experiment would be conducted on straight course, and at many combinations of path curvature and drift angle.

PROGRAM III: Pure-Yaw-Rotation Experiment

A 5-ft model was moved in pure yaw rotation by applying a known yaw moment via falling weights and pulleys. The resulting steady yaw rate was measured. A Series 60 model was used; particulars of which are given in Table I.

A vertical mast was erected in the model coincident with the model's negative z-axis (through the CG). The mast was a drum having two fine cords attached, which, when wound around the drum, applied a pure yaw moment. The cords were led over ball-bearing pulleys attached to the outer sides of the walls of Tank No. 3. Weight holders were hung from the cords, and the system was arranged to permit the weights to hang freely and travel downward as the model commenced to rotate.

In testing, the lines were wound about the drum, elevating the weights. When the model had been positioned directly between the pulleys, the model was released. After an acceleration interval, the time of one-half revolution in yaw was measured. Different weights permitted a determination of the effect of yaw rate on the dimensionless moment coefficient, $\frac{N}{\frac{\rho}{2} \, L^4 H \, r^3} \cdot \text{Results are plotted in Figure 9.} \quad \text{These show}$ regligible change of coefficient value over the reange of the test.

COMPUTATION OF SIMPLE DOCKING MANEUVER

General

The equations of ship motion (16 through 20) were programmed for numerical integration by digital computer. The computer source program written in Kingston Fortran language, is listed in Appendix B. The program applies to calculation of various turning, stopping, and accelerating maneuvers of a single-screw ship.

An example application of the mathematical model is made in the calculation of a simple docking maneuver; namely, the "one-bell" landing. This maneuver involves a single engine reversal to halt a ship alongside its berth. The particular purpose is to demonstrate sensitivity of ship response to operating and design parameters. Conditions of the maneuver are idealized in the sense that no tugboat or MPD forces are applied, no wind acts, and deep-water hydrodynamic coefficients are used. The one-bell landing is a legend for large ships, but as a limit maneuver it provides insight into the docking problem.

Characteristics of the study ship are given in Table I. Hull dimensions approximate the MARINER's, but are based on a Series 60 form. Coefficient values are listed in Table IV and values of other parameters in Table V. Conventional Y and N hydrodynamic derivatives are obtained from Reference 13 (Model 60).

To extend the results of computations to ships of other sizes, the following scaling laws may be used: Subscript A refers to the study ship, and B to a geometrically similar ship of different size. The factor λ is the scale r_i to based on length; i.e., $\lambda = L_B/L_A$. Typical examples of scaling are shown.

Distance:	x _B = x _A x λ	Linear acceleration:	ů _B = ů _A x 1
Angle:	$\psi_{B} = \psi_{A} \times 1$	Angular acceleration:	$\dot{r}_B = \dot{r}_A \times \lambda^{-1}$
Time:	$t_B = t_A \times \lambda^{1/2}$	<pre>Speed (ship and current):</pre>	$u_{-} = u_{-} \times \lambda^{1/2}$
Force:	$X_B = X_A \times \lambda^3$,
Moment:	$N_B = N_A \times \lambda^4$	Angular speed:	$n = n \times \lambda^{-1/2}$

The correlation of hydrodynamic terms between models of different size (and especially between model and ship) is a major problem in ship hydrodynamics. For this reason a 14-ft-long model was used to measure forces depending on rudder actions, and friction scale effect was accounted for in scaling thrust forces. Still, the main interest of the work is to extend ship motion analysis to permit evaluation of parameters affecting maneuvering performance at low speeds, and not the precise determination of ship response.

The basic conditions of the example maneuver are these:
The ship approaches a pier at a constant velocity of 4.3 knots, relative to the water. This corresponds to a propeller speed of 20 rpm. Turning rate and drift angle are initially zero. The "full astern" command is executed, and subsequent ship motions and trajectory are computed.

The calculation is repeated for several variations of each of the following parameters:

- 1. Maximum reversed propeller speed, n*
- 2. Propeller-response time lag, i.e., time constant T
- 3. Velocity of uniform water current, \overrightarrow{U}_{c_0}

With propeller reversed at low ship speed, rudder deflection was found to have negligible effect on ship motion and trajectory; hence, it is not included as a parameter in these computations.

Distance and time required to stop are used as performance criteria for studying sensitivity to parameters 1 and 2. For parameter 3, the lateral trajectory characteristics, position and velocity, are used.

The computation proceeds from t_0 , when the command n^* to propeller is given. Formally, the initial conditions of motion are u = u(0), $v = r = \dot{u} = \dot{v} = \dot{r} = 0$. Initial heading, $\psi(0)$, is arbitrary unless water current is specified. Coordinates $x_0(0)$ and $y_0(0)$ are also arbitrary. Typical computer output is shown in Appendix C.

Results.

The effects of maximum reverse propeller speed are shown in Figure 10. Clearly, variations of $n^{\frac{1}{2}}$ about the base value of -45 rpm cause significant

variations in head-reach and time-to-stop. For the study ship, -45 rpm corresponds to normal "full astern." This is the command most likely to be used for killing headway of a fully loaded vessel. The response to emergency full-astern (taken as -60 rpm) is significantly quicker, and responses to lower values such as half-astern (-30 rpm) are unacceptably sluggish for docking. The curves representing time-and distance-to-stop are similar in character under these conditions. This is in accord with the simplified relations between constant retarding force, X, and the time and distance necessary to destroy kinetic energy. Energy and motion equations yield

$$s = -\frac{(m-X_{\dot{u}})u_{\dot{o}}^{2}}{2X}$$
 and $t = -\frac{(m-X_{\dot{u}})u_{\dot{o}}}{X}$

At low ship speeds, X is mainly determined by n^2 ; hence, both s and t are proportional to $1/n^2$.

Figure 11 indicates how response time of the engine affects distance and time-to-stop. Since the time constant T is a measure of delay in achieving \mathbf{n}^{*} , it dictates delay in reaching peak deceleration. This affects distance covered in each succeeding increment of time after \mathbf{t}_{0} . Time-to-stop is not correspondingly affected, however.

The validity of the longitudinal ship-motion calculation was tested by computing stopping maneuvers of the ESSO SUEZ and comparing results with full-scale test data reported by Hewins, Chase, and Ruiz. 19

Ship trajectories corresponding to three variations of the basic docking maneuver are pictured in Figure 12. Water current is the parameter. A time history of significant computational variables for the no-current condition is shown in Figure 13. Computed yaw-angle and drift-angle values develop significantly prior to ship stopping. Measurements of free maneuvering are unavailable for verification of these results, but tendencies appear to be correct, based on experience with full-scale ships. The general preference of ship-handlers for port-side-to-pier landings is based on these effects (for right-hand single-screw ships).

Trial computations were made to discuss the importance of steadystate hydrodynamic terms in low-speed transient maneuvers. These showed that elimination of all steady-state hull terms did not appreciably affect the longitudinal motion results shown in Figure 13. However, effects on lateral motions were quite large, roughly doubling the values of yaw angle, drift angle, and lateral displacement. In another trial, only linear hull hydrodynamic terms were included. Results more in line with the basic computation were then obtained. However, it is cautioned that the simple docking maneuver does not involve large drift angle or (dimensionless) turning rate through most of the duration, as might be the case in other low speed maneuvers.

The effect of uniform water current on a slowly moving ship is important. In Figure 12 the effect of a one-knot current, setting east, is compared to a one-knot current setting west (relative to a north-south pier). The right-hand ship is set heavily westward and put hard against the pier. The left-hand ship is set eastward, and finds that a portside-to-pier landing is impossible. Therefore a starboard-side landing is shown. Because uniform water current adds a constant velocity to other ship motions, time-to-stop is very important in water-current cases.

A limiting criterion for docking is contact velocity with the pier. Lateral contact velocities of -2.3 feet per second (for the ship set westward in Figure 12) or 1.1 feet per second (for the ship set eastward) could result in costly side-shell damage. A realistic non-uniform current would be weaker near the pier, and more confused, but the desirability of having additional lateral control forces available is apparent.

Combined with yaw rotation, the lateral velocity at the stern (at station 18, on 20 stations) is -2.7 feet per second.

CONCLUSIONS

Conclusions of this study are based on experimental results, results of computed maneuvers, and mathematical model development.

Conclusions Based on Experiments

- 1. Straight-course experiments show that the speed of an ahead-turning propeller strongly influences rudder effectiveness of a single-screw ship. The relation may be expressed in terms of the propeller advance ratio J_s for ahead ship motions. When propeller rotation is reversed, rudder forces are small, erratic, and ineffective for control.
- 2. A significant side force is generated by the rotation of a single propeller behind a ship, especially for reversed propeller rotation at low ship speeds. This force is responsible for a tendency toward positive (clockwise) yaw rotation during ship-stopping. The ratio of measured yaw moment to side force locates the center of effort at approximately 10%L forward of the rudder post, for reverse propeller rotation, and approximately at the position of the rudder for ahead propeller rotation.
- 3. Hydrodynamic yaw moment resulting from pure yaw rotation is closely proportional to the square of yaw rate for a 5-foot Series 60 model at yaw rates between 0.04 and 0.07 sec⁻¹.

Conclusions Based on Computed Maneuvers

- Computations show the importance of maximum reverse propeller speed, n*, in ship stopping from low speeds. Since hull resistance is minor at low speeds, the stopping force is mainly determined by n* squared.
- 2. The time response of the engine importantly affects the speed with which astern thrust, hence ship deceleration, is established. Since this affects the duration of the high-speed part of the maneuver, it has

much greater effect on distance than on total time required to stop.

3. For some maneuvers, time-to-stop is more important than distance. For example, ship translation due to a uniform water current depends directly on total elapsed time, and not at all on distance traveled through the water. Therefore, a maneuver which may be simple for an unassisted ship in still water could be impossible in a modest current, depending on the time it takes to complete.

Conclusions Based on Development of Mathematical Model

- 1. Propeller forces are conveniently represented in motion equations by following the familiar k_t vs. J_s notation. Extension of the k_t , J_s concept assists in the representation of longitudinal force, lateral force, and yaw moment, as convenient functions of ship speed, propeller rotation, and rudder angle. Applied to both ahead and reverse propeller rotation, the technique provides insight into the changing propeller flow conditions. After blade stall, a locked propeller drag function may suffice until stall recovery. Computations may be organized on the basis of instantaneous J_s value.
- 2. If the water current can be assumed uniform, vector addition of ship motion through the water and motion of the water current permits a considerable simplification of the equations of motion. On the other hand, if water current is so irregular as to disallow this assumption, mathematical representation may be impractical.
- 3. In general, the variety of ship motions possible at low ship speed is boundless. Because of this, appropriate force and moment data are necessary in computations of low-speed ship maneuvers. Steady-state hydrodynamic reactions are complex functions which cannot be arbitrarily excluded from ship-motion equations, even at low ship speeds.

The mathematical model is a useful tool which may be extended to include additional forces, such as wind and auxiliary propulsion devices. Constraints due to anchor or mooring lines may be added. With the proper data on external forces, the mathematical model provides an excellent means for analyzing many complex problems associated with low-speed ship maneuvers.

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TABLE I MODEL AND SHIP CHARACTERISTICS

HOULE A	arb only change	JIERIGII I S	
HULL	14-FT MODEL	5-FT MODEL	SHIP
Length, BP, L , ft	14.00	5.00	528.5
Breadth, B , ft	1.868	0.714	75.5
Draft, H , ft	0.747	0.267	28.2
Block Coefficient, C _b	0.60	0.60	0.60
L/B	7.50	7.0	7.0
L/H	18.75	18.75	18.75
Displacement, A	731 1b F.W.	35.61b F.W.	19,300 L.T.
L x H , sq ft	10.46	1.335	14,900
Lateral Area of Hull, sq ft	10.35	1.320	14,750
Mass of Model, M , slugs	22.75	1.11	1,345,000
LCG/L from FP	0.515	0.515	0.515
Radius of Gyration in Air, ft	:		132.1
RUDDER			
Area of Rudder, A _p , sq ft	0.167	0.021	238
A _P /LH	0.016	0.016	0.016
Aspect Ratio of Rudder	1.90	1.90	1.90
PROPELLER			
Troost - 4 blades			
Diameter, d , ft	0.518	0.198	19.54
Pitch, p , ft	0.599	0.187	22.50
p/d	1.15	0.95	1.15
Mean Width Ratio, MWR	0.261	-	0.261
Expanded Area Ratio, EAR	0.550	-	0.550
Blade Thickness Fraction, Btf	0.045	-	0.045
Rake, deg	6	-	6

TABLE II STRAIGHT-COURSE FORCE AND MOMENT DATA

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RUN NO .	u	n	δ	X	Y	N
	fps	rps	deg	16	16	1b-ft
103	•00	7.65	U	4.14	06	-50
101	• 00	7.65	10	4.14	• 41	-2.98
99	• 00	7 • 65	20	3.44	• 77	-5.58
097	• 00	7.60	30	3.64	64	-7.08
105 107	• UU	7•65 7•65	-10	4.20	98	4.24 6.50
109	• 00	7•65	-30	J.80	-1.17	7.78
71	•46	7.65	υ	3.50	07	•45
90	•86	7.65	10	3.54	•61	-4.12
42	.86	7.65	20	2.33	1.06	-7.72
44	•85	7.65	30	3.03	1.48	-10.30
43	•54	4.61	30	.91	فرق و ماريخ	-2.64
72 78	•86 •86	7 • 65 7 • 70	-10 -20	3.04 3.33	70 -1.25	4•73 8•34
84	•86	7•10	-30	2.03	-1.69	10.56
44	•68	4.59	30	•69		-2.90
64	•86	4.59	U	1.11	-•08	• 24
58	•89	4.01	10	1.05	• 25	-1.80
52	•86	4.55	Z'U	1.01	• 44	-3.02
50	⊌84	4.54	٥٥	•61	• 44	-3.91
45	• 88	4.59	٥٥	•69	• 33	-3.17
79	•86	4.59	-20	1.01	49	3.61
85 104	•86 •00	4 • 59 = 7 • 65	-30	•01 -2•75	- 68 - 68	4.62
102	•00	-7.65 -7.65	0 10	-2.75	-•52 -•62	J.44 J.46
100	•00	-7.65	20	-2.73	-•66	3.96
98	•00	,-7.65	30	-2.83	60	3.81
106	•00	-7.65	-10	-2.64	27	3.65
108	•00	-7.65	-20	-2.63	64	3.14
110	•00	-7.65	-30	-2.61	-•78	4.32
70	•86	-7.65	Ü	-3.43	69	3.01
91	•86	-7.65	10	-3.33	-1.23	4-62
93 95	•86 •85	-7•65 -7•65	20 30	-3.43 -3.43	-•88 -•61	2•27 3•98
77	•86	-7.66	-10	-3.03	34	1.90
83	•86	-7.67	-20	-2.93	61	3.17
89	•86	-7.65	-30	-3.03	74	3.41
69	•86	-4.56	U	-1.21	25	1.25
63	•86	-4.59	10	-1.31	15	•88
57	•86	-4.52	20	-1.31	35	1.24
51	•85	-4.61	30	-1.21	37	1-17
76 82	•86 •86	-4.59 -4.62	-10 -20	-1.11 -1.21	-•15 -•13	1.53
88	•86	-4.52	-30	-1.41	16	• 46 • 85
152	4.20	7.66	Ü	61	04	•01
154	2.79	4.96	O	30	03	11
159	4.26	7.42	U	-1.11	30	.34
160	4.23	7.44	U	47	09	•46
165	4.23	7.42	O	-1.01	16	•23
151	4.20	7•35 4•76	O	91	03	•11
167 155	2•79 5•65	7.54	U	30 -3.84	04	•23 ••42
161	4.23	4.75	Ö	-2.32	15	14
153	2.79	4.53	Ü	51	09	•05
156	5.65	4.91	ŭ	-5.45	19	63
169	1.44	-4.49	U	-1.11	07	•10
168	2.79	-7.42	U	-2.71	23	•33
164	4.23	-7.47	U	-5.47	• 23	-2.4
166	2.79	-4.51	Ü	-2.12	•01	53
163	4.23	-4.41	O	-4.55	09	10
158	5.65	-4.45	U	-8.69	-•26	•86

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TABLE III STRAIGHT-COURSE DATA IN COEFFICIENT FORM

RUN NO.	Js	Kx	KY	K _N	So	Υ'	N'
103	•00	•508	01	•12	1.000		
101	• 00	•508	•05	71	1.000		
99	• 00	• 483	• 10	-1.30	1.000		
97	• 00	·45J	• 1 4	-1.70	1.000		
105	• 00	•516	-•08	1.01	1.000		
107	• 00	.491	- • 1 4	1.54	1.000		
109	• 00	• 466	- • 1 4	1.84	1.000		=
71	• 2 2	•442	01	• 1 1	• U L L	01	• 00
92	• ८ ८ • ८ ८	. 447	•U7	+•98 -1•83	•원1년 •원1년	• 05 • 14	U4 U7
94	• 21	• 797 455	• 18	-2.44	-815	-20	10
43	.23	• J 1 U	•11	-1.73	• EU4	•11	06
72	.22	•460	09	1.12	•812	09	.05
78	.22	•418	-•15	1.75	.813	17	• 08
84	• ८ ८	• J54	- • 4 1	2.44	•813	-023	.10
44	.29	0363	• 1 1	-1.91	· 753	• 47	04
64	• 36	•416	-•03	•19	• 687	01	•00
58	•37	6247	•∪8	-1.18	"617	ق () ه	-•02
54	• 36	• 264	• 15	-2.03	•666	• 06	-•0
50	٠ كان	د عده	•17	-4.66	• 690	• 07	04
45 79	• 37	• 474	• 1 1 - • 1 7	-2.09	• 682 • 432	• 04	03
85	• 36 • 36	• ୬ ೮८	-•17 -•25	4: • JU 4: • 7U	•687 •687	-•07 -•09	•UJ
104	•00	- 0 J J 7	-•06	•82	1.000	- • • •	•04
102	•00	337	-•08	•82	1.000		
100	•00		-•08	•94	1.000		
98	•00	347	07	•90	1.000		
106	• 00	325	03	•87	1.000		
108	• 00	-0366	-•UB	• 76	1.000		
110	• 00	320	05	1.02	1.000		
70	-•22	- • 408	09	•71	1 • 1 6 8	09	•03
91 93	- • ¿ ¿	-•787 -•786	-•15 -•U7	1.10	1 • 188	-•16 -•08	• 04
95	-021	-•4UB	11	•54 •94	1 • 185	12	•UZ
77	-022	-•358	- • 0 4	• 45	1.167	-•05	•02
83	-022	345	07	. 75	1.187	-•08	•03
89	22	158	09	• 81	1.108	10	.03
69	-•36	160	09	•83	1.315	03	•01
63	36	410	05	• 58	1.313	02	•01
57	37	463	12	• 64	1.316	05	•01
51	- • 36	-0312	-•13	• 76	1.308	05	•01
76	- • 36	341	12	1.00	1.313	-•05	•01
873	- 0 36	-0371 -0370	04	• 6 4	1.311	02	• 0 1
152	1.06	-6378	•00	• 56	6 L C O L C C C C C C C C C C C C C C C C	-•UZ •UU	• U 1
154	1.08	.209	01	06	• 00Z	• 00	•00
159	1.10	158	04	•10	•050	• 00	•00
160	1.10	• 176	01	.12	• 050	• 00	•00
165	1.10	•171	02	•06	•U4B	• 00	• 00
151	1.10	• I 85	•00	•03	. 046	• 00	• 00
167	1017	• ८ ८ ४	01	• 14	•021	• 00	• 00
155	1.45	•067	01	75	- • 252	• 00	• 00
161	1.74	• 000	05	19	- 486	• 00	• 00
153	1.19	-180	- • 0 3	- 44	-•920 -•028	• 00	•00
164	2022 -062	-0214 -0289	-•Us	-•36 •∪7	1.520	• 60	•00
168	73	-0207 -0261	-•03	•08	1.524	• 00	•00
164	-1.09	406	•03	62	1.945	• 00	•00
166	-1020	390	•00	36	2.034	• 00	•00
163	-1.85	064	03	07	2.602	• 00	• 00
158	-2.45	-1.512	09	•61	3.122	• 00	•00

TABLE IV

COEFFICIENT VALUES FOR SHIP IN SIMULATED MANEUVERS

XI	0068	Y ₃	0062
X	0075	b _o	010
x _{vr}	.168	b ₁	0326
a _o	.494	p ⁵	. 291,
a ₁	231	b ₃	-397
a ₂	043	b ₄	•12
a ₃	141	b ₅	.0127
a ₄	322	b_{e}	080
a ₅	059	NÏ	0107
a ₆	_	N.	095
a ₇	.300	N'r	070
a 8	.600	1/2(Nrv+Nr)	-1.43
a ₉	325	1/2 Nrr	127
a ₁₀	.500		304
a ₁₁	1.50	1/6(N_''+3N'')	061
a _{1 2}	1.00	N ₁	095
Y.i	168	N ₂	169
Y	305	N ₃	525
Y	.085	c _o	.15
1/2(Yrvy+Y')	614	c ₁	-3.85
1/2 Y 1	-1.15	c ⁵	-4.41
1/6 Y	-3.20	c ₃	-2.62
1/6(Y, '+3Y')	.101	c ₄	0061
Y ₁	305	c ₅	•79
Ya	65		

TABLE V

FIXED PARAMETERS IN EXAMPLE COMPUTATIONS

rt = 1.000

 $\beta_{L} = .262 (15^{\circ})$

u_L = .845 fps

g₁ = .376

 $g_2 = -.158$

 $g_3 = -1.00$

 $\Delta t = 1.0 \text{ sec(iteration time)}$

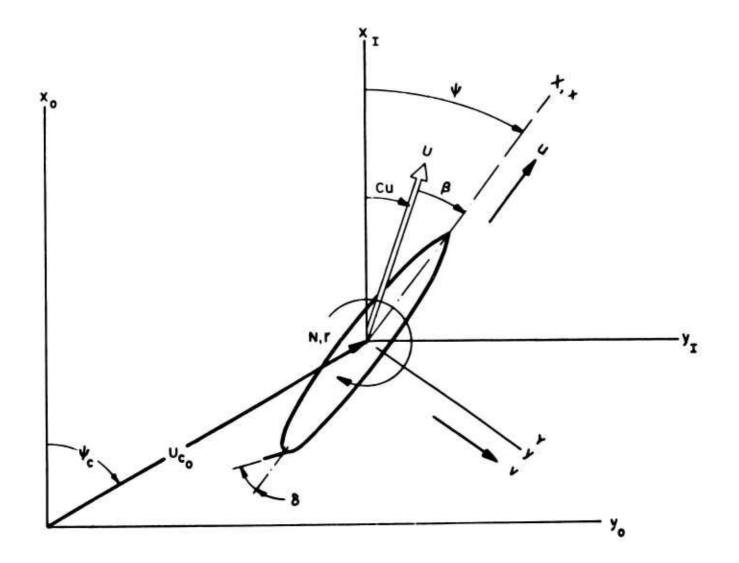


FIGURE I. REFERENCE FRAMES

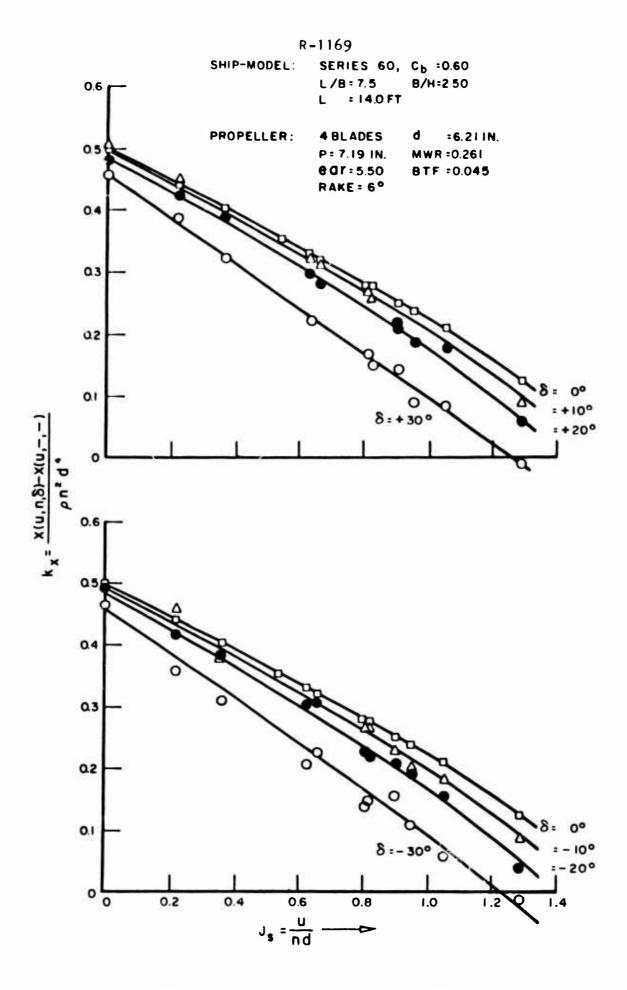


FIGURE 2. VARIATION OF LONGITUDINAL FORCE COEFFICIENT k_{χ} , WITH RUDDER ANGLE AND PROPELLER ADVANCE-RATIO IN BEHIND-SHIP CONDITION

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1

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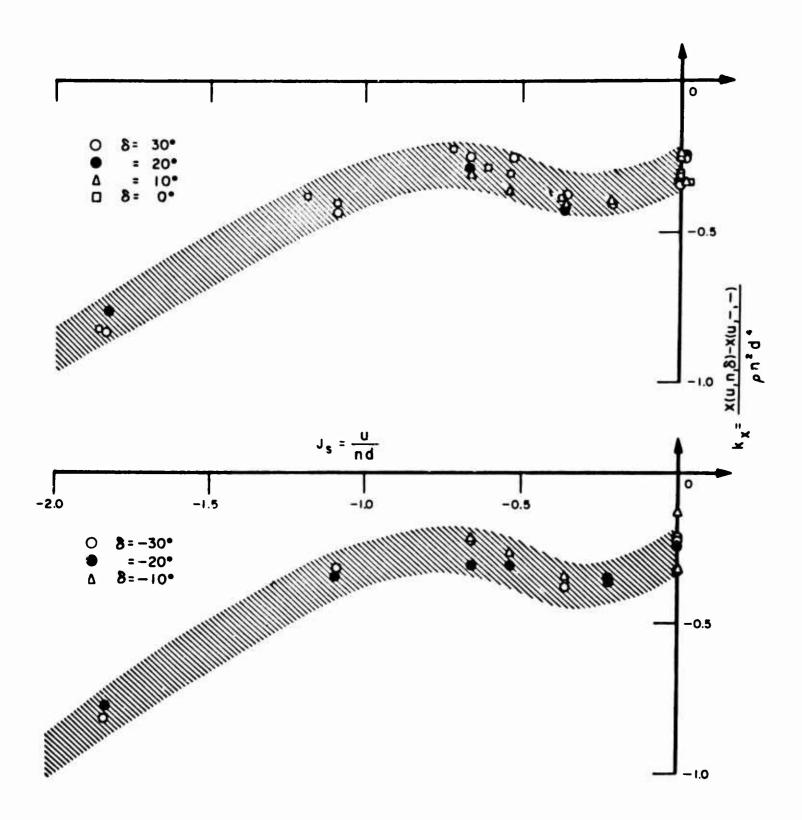


FIGURE 3. VARIATION OF LONGITUDINAL FORCE COEFFICIENT k_χ , WITH RUDDER ANGLE AND ADVANCE RATIO OF PROPELLER IN BEHIND-SHIP CONDITION, J_s =u/nd (u> o, n<o)

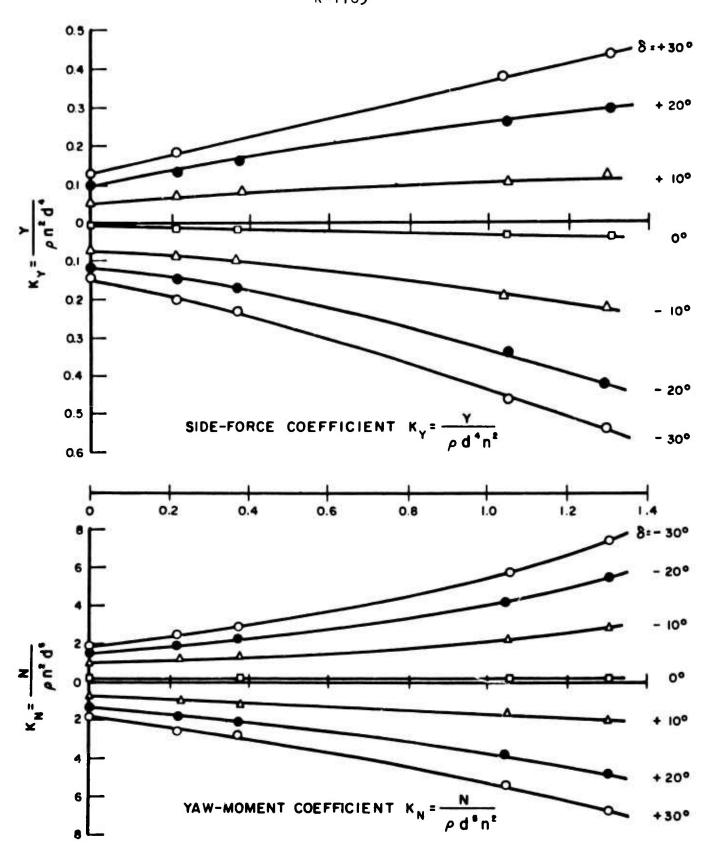


FIGURE 4. VARIATION OF SIDE-FORCE AND YAW-MOMENT COEFFICIENTS WITH RUDDER-ANGLE AND PROPELLER ADVANCE-RATIO IN BEHIND-SHIP CONDITION $J_s = \frac{U}{nd}$

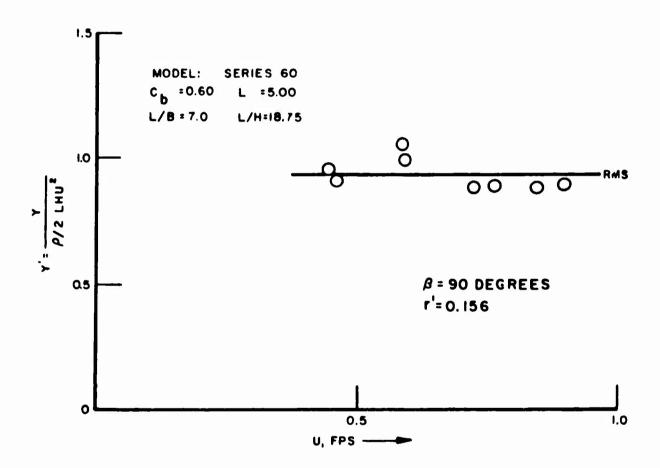


FIGURE 5. EFFECT OF MODEL SPEED ON SIDE-FORCE COEFFICIENT, Y'

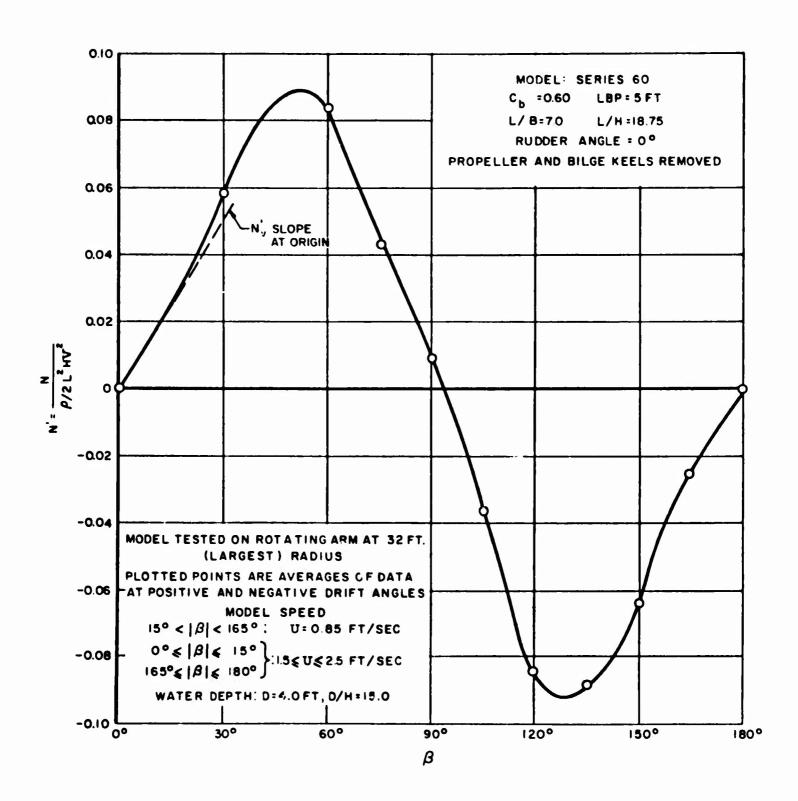
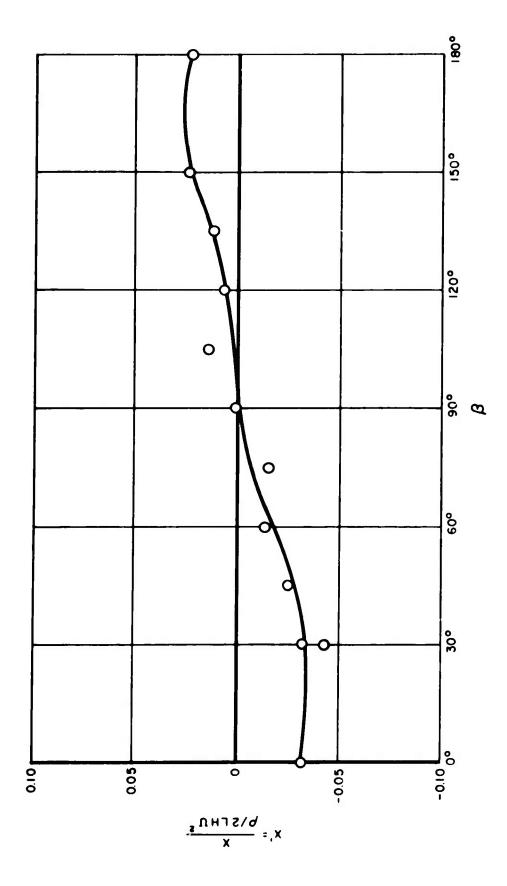
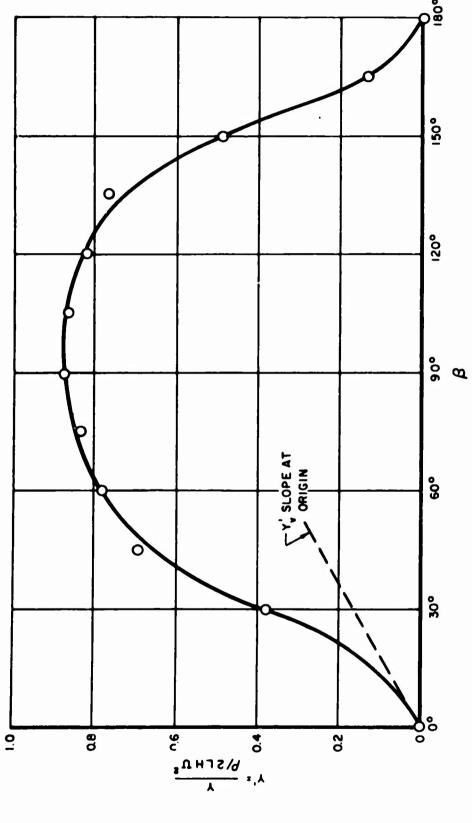


FIGURE 6. YAW MOMENT COEFFICIENT VERSUS DRIFT ANGLE (MOMENT AXIS THROUGH MODEL C.G. - 0.015 L AFT OF)

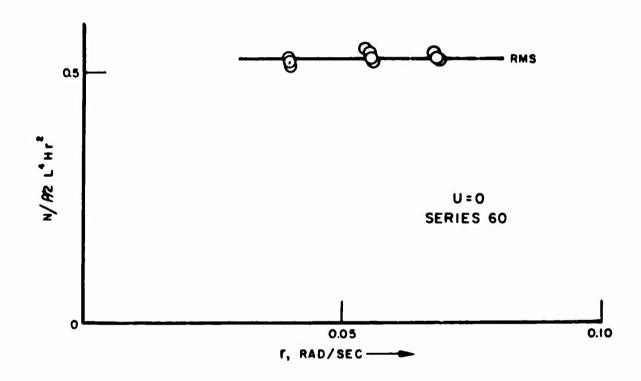
×



LONGITUDINAL FORCE COEFFICIENT VERSUS DRIFT ANGLE FIGURE 7.



SIDE FORCE COEFFICIENT VERSUS DRIFT ANGLE FIGURE 8.



COEFFICIENT, N/p/2 L + Hr 2

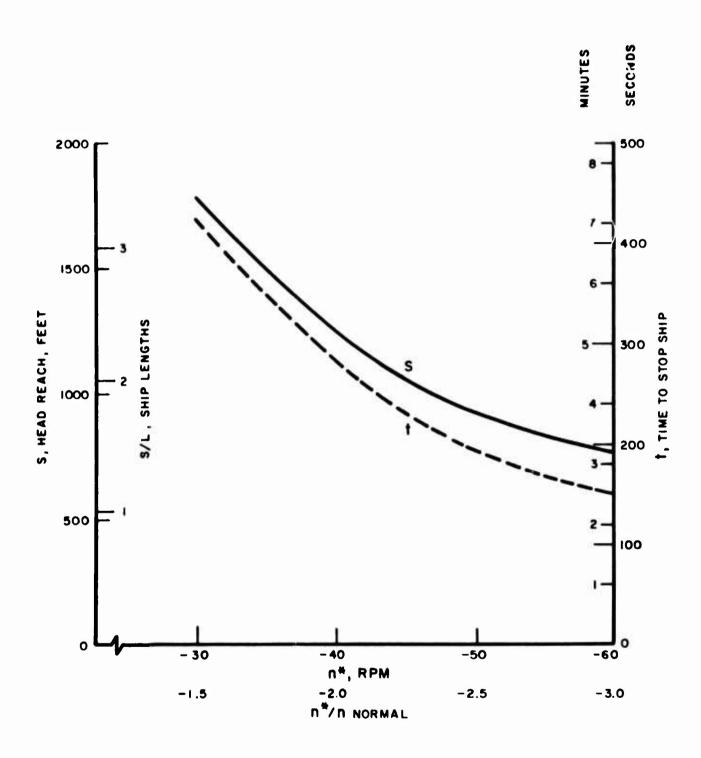


FIGURE 10. EFFECT OF REVERSED PROPELLER-SPEED ON DISTANCE AND TIME REQUIRED TO STOP SHIP FROM 4.3 KNOTS (COMPUTATION OF SIMPLE DOCKING MANEUVER)

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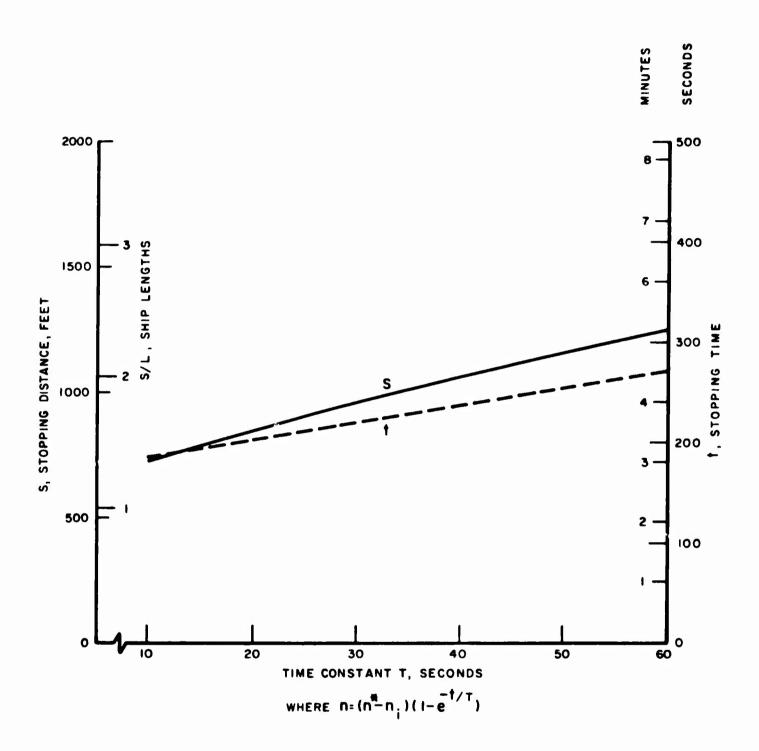


FIGURE II. EFFECT OF ENGINE-RESPONSE LAG ON DISTANCE AND TIME REQUIRED TO STOP SHIP FROM 4.3 KNOTS (COMPUTATION OF SIMPLE DOCKING MANEUVER)

1

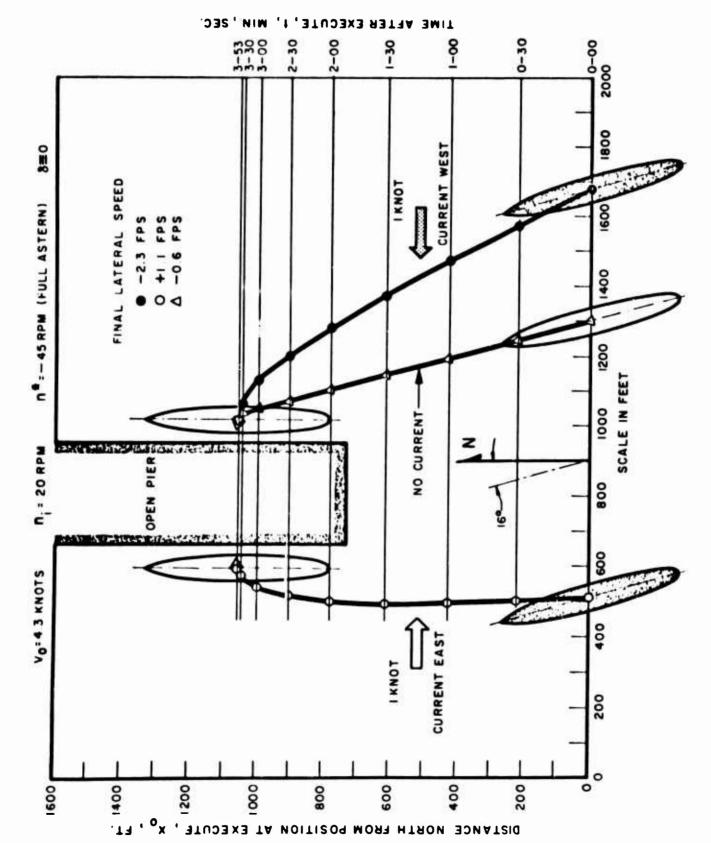


FIGURE 12. COMPUTED RESPONSE OF CARGO SHIP FOR SIMPLE "ONE BELL" LANDING



4. 1

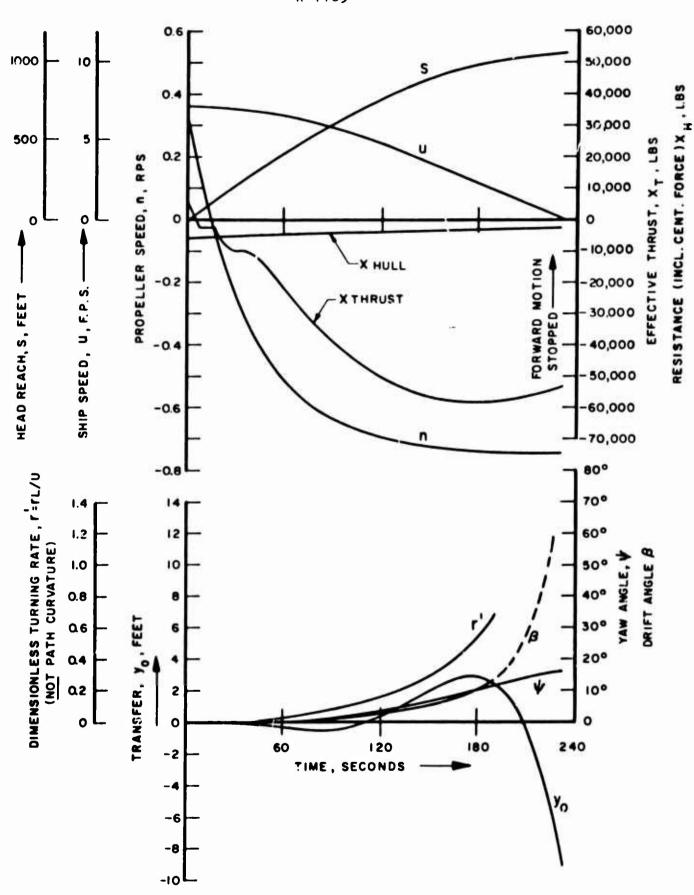


FIGURE 13. COMPUTED TIME-HISTORY OF PRINCIPAL VARIABLES IN TYPICAL DOCKING MANEUVER

APPENDIX A

Drag of Locked Propeller

In the operating region between 4 and 6 of Sketch I, page 12, the propeller force is essentially a drag force associated with propeller blades continuously changing orientation and angle of attack with respect to local flow. In the absence of detailed experimental data, a simple drag coefficient for a locked propeller can suffice. This may be estimated on the basis of developed blade area, DAR, ship speed, u, and mean wake fraction in way of the propeller, w.

$$X(prop.)_{dragging} = C_D \frac{\rho}{2} A u_P^2$$

$$= C_D \frac{\rho}{2} \times DAR \frac{\pi d^2}{4} \times \left[u(1-w) \right]^2$$

$$= \rho d^2 a_5 u^2$$

where

$$a_6 = C_D \times DAR \times \frac{\pi}{8} \times (1-w)^2$$

Estimations of $C_{\rm D}$ for ship propellers are discussed in Reference 19.

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APPENDIX B

COMPUTER PROGRAM FOR SIMPLE ENGINE- AND-RUDDER MANEUVERS

```
C
      KINGSTON FORTRAN 2. 1620. STEVENS
      DIMENSION C(12.7)
    1 READ 100.((C(1.J).J=1.7).1=1.12)
      PUNCH 100
      PUNCH 101 + ((C(1+J)+J=1+7)+1=1+12)
      PUNCH 102
      CONL1=C(1+3)*C(1+4)*C(1+5)/2+0
      CONL2=CONL1*C(1+4)
      CONL3=CONL2*C(1+4)
      CONL 4 = CONL 3 * C (1 + 4)
      CONL 5=CONL 4*C(1.4)
      COND1=C(1+3)*C(1+6)
      COND2=COND1*C(1.6)
      COND3=COND2*C(1.6)
      COND4=COND3*C(1+6)
      COND5=COND4*C(1+6)
      AO = C(1 + 1) - CONL2 * C(3 + 1)
      A1=CONL1*C(3+2)
      A2=C(1.1)+CONL2*C(3.3)
      A3=COND4*C(3+4)
      A4=CQND3*C(3+5)
      A5=COND2*C(3+6)
      A6=COND4*C(3.7)
      A7=COND3*C(4+1)
      A8=COND2*C(4+2)
      A9=CONL1*C(4+3)
      A10=CONU4*C(4+4)
      A11=COND3*C(4.5)
      A12=COND2*C(4.6)
      A13=COND1*C(4.7)
      A14=COND4*C(9+6)
      A15=COND3*C(9.7)
     B0=C(1.1)-CONL2*C(5.1)
     81=CONL1*C(5+2)
     B2=CONL2*C(5+3)-C(1+1)
     83=CONL2*C(5+4)
     B4=CONL3*C(5+5)
     H5=CONL1#C(5+6)
     BG=CONL4*C(5+7)
     H7=CONL1*C(6+1)
     BB=CONL1#C(6+2)
     B9=CONL2*C(6+3)-C(1+1)
     B10=COND4*C(6+4)
     B11=COND2*C(6+5)
     B12=COND4*C(6+6)
     B13=COND3*C(6+7)
     H14=COND2*C(7+1)
     B15=CONL1*C(7.2)
     B16=COND4*C(7.3)
     CO=C(1.2)-CONL4*C(7.4)
     C1=CONL2#C(7+5)
     C2=CONL3*C(7.6)
     C3=CONL3*C(7.7)
     C4 = CONL 4 * C (P+1)
     C5=CONL2*C(8+2)
     C6=CONL5*C(8+3)
     C7=CONL2*C(8+4)
```

```
CA=CONL2*C(8.5)
   C9=CONL4+C(8+6)
   C10=COND5#C(8+7)
   C11=COND5#C(9:1)
   C12=COND4#C19+21
   C13=C0ND3+C(9+3)
   C14=CONL2#C(9+4)
   C15=COND5+C(9+5)
   YMPD=C(12.1)
   ENMPD=YMPD*C(12+2)*C(1+4)
   J=1
   T=C(11.5)
   U=C(10.1)
   V=C(10.2)
   UG=C(10.1)
   VG=C(10.2)
   R=C(10.3)
   RPSD=C(10.5)
   DEL=C(10+6)
   DELD=C(10.7)
   DELDOT=C(11.1)
   X=C(11.2)
   Y=C(11.3)
   S=C(2.7)
   PSI=C(11.4)
 7 W=SQRTF (U#U+V#V)
   RPR1=P*C(1.4)/W
   SRPRI = AUSF (RPRI)
   HETA = - ATANF (V/U)
   SHETA=AUSF (HETA)
   RPS=C(10+4)+(RPSD-C(10+4))+(1+0-EXPF(-(T-C(11+5))/C(1+7)))
   IF (SPPRI-C(2+2)) 50+50+51
50 IF (SBETA-C(2+3)) 52+52+51
52 IF (U-C(2+4)) 51+53+53
53 XHULL = A1 #U #W + A2 #R #V
   YHULL=81*U*V+82*U*R+83*R*V*#2/U+84*V*R**2/U+85*V**3/U+86#R**3/U
   ENHUL =C1*U*V+C2*U*R+C3*R*V**2/U+C4*V*R**2/U+C5*V**3/U+C6*R**3/U
   GO TO 3
51 XHULL = A1 + U + W + A2 + R + V
   YHULL=B7*V*W+B8*V*ABSF(V)+B9*U*R
   ENHUL = C7*U*V+C8*V*U*ABSF(V*U)/W**2+C9*R*ABSF(R)
 3 RJ=RP5*C(1+6)/U
   IF (RJ-+376) 60+60+61
60 IF (RJ++158) 63+63+62
63 IF (RJ+1.0) 65.65.64
61 XCONN=A3*RPS**2+A4*U*RPS+A5*U**2+(A6*RPS**2+A7*U*RPS)*DEL**2
   YCONN=810#RPS##2+811#U##2+(812#RPS##2+813#U#RPS+814#U##2)#DEL
   ENCON=C10*RPS**2+(C11*RPS**2+C12*U*RPS+C13*U**2)*DEL
   GO TO 4
62 XCONN=A8+U+W+A9+U++2+DEL++2
   YCONN=815#U##2#DEL
   ENCON=C14#U##2*DEL
   GO TO 4
64 XCONN=A14*RPS**2+A15*U*RPS
   YCONN=B16*RPS**2
   ENCON=C15*RPS**2
   GO TO 4
65 XCONN=A10*RPS**2+A11#U#RPS+A12#U**2+A13#U**3/RPS
   YCONN=B16#RPS##2
   ENCON=C15#RPS##2
```

```
4 UDOT=(XHULL+XCONN+C(2.5))/AO
    VDOT = (YHULL+YCONN+YMPD) /80
    RDOT = (ENHUL+ENCON+ENMPD)/CO
    PD1=57.28*PS1
    BEDA=57.28*BETA
    DED=57.28*DEL
    ST=T#0.1
    JT=ST
    JT=JT#10
   JT=JT+1
    IF((JT/J)-1) 6.5.6
  5 PUNCH 103+T+PDI+U+X+Y+BEDA+RPRI+RPS+DED+XCONN+XHULL+UDOT+UG+VG+S
  6 U=U+UDOT*C(2+1)
    V=V+VDOT*C(2+1)
    R=R+RDOT*C(2+1)
    PS1=PS1+R*C(2+1)
    UG=C(11+6)*COSF(C(11+7))+U*COSF(PSI)-V*SINF(PSI)
    VG=C(11+6)*SINF(C(11+7))+V*COSF(PSI)+U*SINF(PSI)
   X=X+UG*C(2+1)
    Y=Y+VG*C(2*1)
    S=S+W*C(2+1)
    IF(U-C(2.6)) 71.70.70
70 IF (ABSF(DEL)-ABSF(DELD)) 40+41+41
 40 DEL=DEL+C(11+1)*C(2+1)
   GO TO 2
 41 DEL = DELD
 2 T=T+C(2.1)
    J=J+1
   GO TO 7
100 FORMAT (55H
  1/(7E1C+4))
101 FORMAT(12(7E10+3/))
                                                    BETA /66HI RPRIME
                  T PSI
                              U
102 FORMAT (42H
                                          UE VE
                  THRUST
                            RESIST. UDOT
  1 RPS DELTA
103 FORMAT (F5.0.F7.1.F7.2.2F8.1.F7.2/1H1.2F7.3.F6.1.F10.0.F9.0.3F7.3.
  1F8.1)
71 GO TO 1
   END
```

NOTE: Program allows inclusion of additional constant control forces in lateral and longitudinal directions, YMPD, NMPD, and XEX. These were made zero in the present study.

820.1 863.0

901.7 936.2 964.4 013.8 031.1

992.2

--251

1 - 095

•327

--040

140.-

-2557 -2525

1.499

--043

-2918 -2639

-57715 -56674

--743

26.95

8.09

025.3

.43 000

15.9 14.0

190 200

170.

5.1

220.

72207

713.3

487.2 550.4

•018 -035 •056 600 --003 .054 •020 **0 .022 -.010 --056 -000 --006 --011 440 -.011 3.213 2.350 7.212 7-152 7-056 6.810 6.184 5.896 5.226 3.640 1.919 6.643 6.435 5.575 4.855 4.464 1.058 2.782 6.941 200 **3** = --044 --040 000 -000 -008 --012 -.015 -.019 --023 --027 --034 -.036 -.039 --042 --043 -0044 --044 -0044 --011 -.031 COMPUTER PRINT-OUT FOR DOCKING MANEUVER OF FIGURE -3306--4176 -5846. -5785 -5689 -5538 -5361• -4952 -4702 -4438 -3932• -3720 -3548 -3423 -3344 -3309 -3324 -3284 -5172 0 11 ລິ[°] -10979. -27839. 5916 -2332 -15526. -33683 -38864 -43338• -47135 -52910 -54986• -56570• -58354• -5170 -10036. -21555 -50308 -57686 -58350 -58569. .101E+00 --141E+00 .397E+00 •150E+00 *400E+02 *000E+00 •100E+01 •600E+00 *000E+00 *000E+00 -.143E+01 0 H 0 0 0 00 0 00 0 0 o 0 0 DELTA 0 0 *60 .195£+02 -.636 -.169E+00 -.525E+00 -294E+00 *000E+00 --320E+C: • 300E+00 •00 -.093 -.603 -. 708 --717 -- 725 -- 738 0 --231E+00 --430F-01 •150E+01 -- 701E-01 *000E+00 -.238 --440 -.508 -.562 -.696 -.730 --735 - 351 -.661 -- 741 -.681 11 100 •016 •050 .078 •194 •455 .003 900 •045 101 .127 • 158 .237 •289 .539 •678 .354 --326E-01 -45 rpm .500E+00 -.954E-01 *000E+00 --115E+01 .790E+00 -.750E+C0 *000E+00 +282E+02 11 .03 1.73 3.57 8.36 13.25 •23 1.30 2.24 2.85 4.43 .64 .34 6.75 0.45 5.47 4 --100E-01 •529E+03 .845E+00 •494€+00 -.325E+00 -.614E+CO --107E-01 -.954E-01 --610E-02 •333E+00 *000E+00 c FD ---.3 1.9 = 20 • CCOE+00 •896E-01 -.620E-02 *262E+00 •168E+00 -- BOOE-C1 --6CBE-01 --262E+01 •00CE+00 *COOE+00 • 199E+01 215.2 72.3 353.8 421.0 486.3 549.3 656.B 770.9 817.3 8-659 898.0 96199 987.3 9.609 720.7 93201 008.4 144.1 285.1 =4.3 kt--305E+00 •127E-01 -.304E+00 --650E+00 --441E+01 -- 750E-02 *COOE+00 *C00E+00 .100E+01 --590E-01 7.06 6.64 5.89 4.85 4.05 3.19 7.21 7.15 6.94 6.81 6.43 6.18 5.57 5.22 4.46 3.62 2.75 2.31 1.87 7.5 1.9 2.6 4.3 5.3 6.4 8.8 10.2 11.6 0 3.4 --127E+00 -- 322E+00 --168E+00 • 120E+00 •135E+07 -.680E-02 -- 305E+00 • 000E+00 • 100E+01 -- 385E+01 •725E+01

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An attempt is made to extend at low ship speeds. Experiments a effects of non-equilibrium propel thrust. Other experiments are made large drift angles and pure yaw receptions are experimental results, together with in motion equations, accounting for occurrence of large drift angles a sion and rudder time lags, and the	are made with a ler speeds on a de to explore otation on hul th previous ro or both extremand turning ra	raptive-mrudder for first-ord hydrody tating-are propell tes. Als	nodel to investigate orce and effective der effects of very mamic reactions. The m data, are applied er actions and the controlled are propul-		

trajectory. The equations are programmed for computation, and ship response to a simple docking maneuver is predicted. The computation is repeated several times to examine sensitivity of ship motions and trajectory to variations of operating parameters; namely, maximum reverse propeller-speed, engine response time, and water-current direction.

KEYWORDS SHIP CONTROL: Maneuvering, Steering, Low-Speed Control

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